

1.3 Function NotationWe now use $f(x)$ instead of y

★ Read "f at x" or "f of x"

$$f(x) = y$$

i.e. $y = 2x + 1$

is $f(x) = 2x + 1$

this notation is useful for such things as describing height as a function of time $h(t)$

$$f(x) = x^2 + 2x + 1$$

$$f(x) = 9$$

$$\begin{aligned}
 f(2) &= x^2 + 2x + 1 \\
 &= (2)^2 + 2(2) + 1 \\
 &= 4 + 4 + 1 \\
 &= 9
 \end{aligned}$$

Ex 1: Connecting the height of a ball above the ground with time:

A ball was dropped from a height of 200m and its height above the ground is represented by the following function:

$$h(t) = -5t^2 + 3t + 200$$

 $t = \text{seconds}$
 $y = \text{intercept}$

How would you find the height of the ball at any time?

⇒ Sub in values for t and solve for h Note " t " is time so do not sub in neg. values
Domain should make sense to the question

t	h
0	200
1	198
2	186
3	164

$$= -5(3)^2 + 3(3) + 200$$

$$= -5(9) + 9 + 200$$

$$= -45 + 9 + 200$$

$$=$$

$$= -5(2)^2 + 3(2) + 200$$

$$= -5(4) + 6 + 200$$

$$= -20 + 6 + 200$$

Ex 2: If $f(x) = 2(x - 1)^2 + 3$, find:

$$\begin{aligned}
 \text{a) } f(0) &= 2(0-1)^2 + 3 \\
 &= 2(-1)^2 + 3 \\
 &= 2 + 3 \\
 &= 5 \\
 f(x) &= 5
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } f(4) &= 2(4-1)^2 + 3 \\
 &= 2(3)^2 + 3 \\
 &= 2(9) + 3 \\
 &= 18 + 3 \\
 &= 21
 \end{aligned}$$

$$\begin{aligned}
 \text{c) } f\left(\frac{1}{2}\right) &= 2\left(\frac{1}{2}-1\right)^2 + 3 \\
 &= 2\left(-\frac{1}{2}\right)^2 + 3 \\
 &= 2\left(\frac{1}{4}\right) + 3 \\
 &= \frac{1}{2} + 3 \\
 &= 3\frac{1}{2} \\
 &= \frac{7}{2}
 \end{aligned}$$

$$\begin{aligned}
 \text{d) } f(4) - f(1) &= 21 - (2(1-1)^2 + 3) \\
 &= 21 - (2(0) + 3) \\
 &= 21 - 3 \\
 &= 18 \\
 f(x) &= 18
 \end{aligned}$$

Ex 2 continued: If $f(x) = 2(x - 1)^2 + 3$, find:

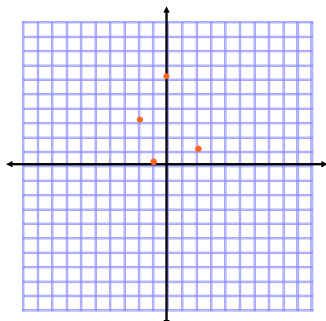
e) $f(3m)$

f) $f(4x)$

$$\begin{aligned}
 &= 2(3m-1)^2 + 3 \\
 &= 2(3m-1)(3m-1) + 3 \\
 &= 2(9m^2 - 3m - 3m + 1) + 3 \\
 &= 2(9m^2 - 6m + 1) + 3 \\
 &= 18m^2 - 12m + 2 + 3 \\
 &= 18m^2 - 12m + 5
 \end{aligned}$$

$$= 22x^2 - 16x + 5$$

Ex 3 Given the graph of f evaluate:



FROM THE POINT
(-2, 3) ←

$$f(-2) = \underline{3}$$

$$f(-1) = \underline{0}$$

$$f(0) = \underline{6}$$

$$f(7) = \underline{NA}$$

Hmwk :

P. 32 # 1, 5 ad, 6 abc, 10a (i,vi), 11- 13

